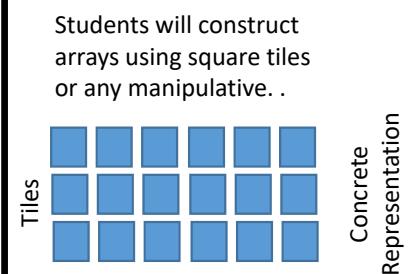
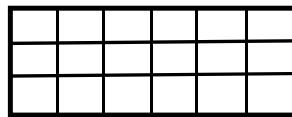


Multiplication starts when students are asked to partition a square 5 by 5.

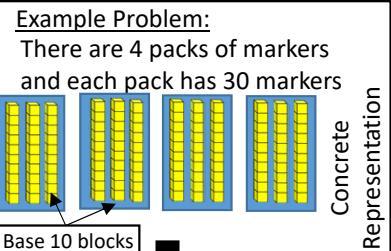
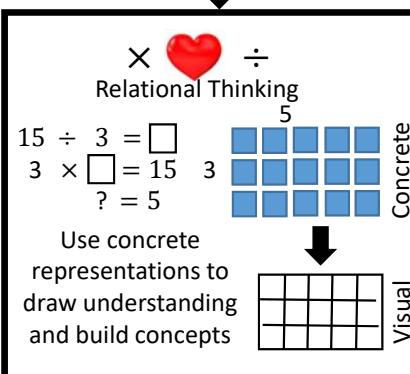
Repeated addition = Multiplication  
 $5 \times 5 = 25$



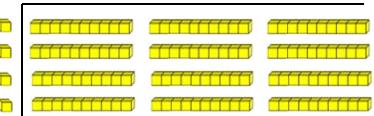
When students create the concrete representations they should also be drawing visual representations as well



Visual Representation



Create an array / Area model



Then group

120 or 12 tens

Pictorial Representation

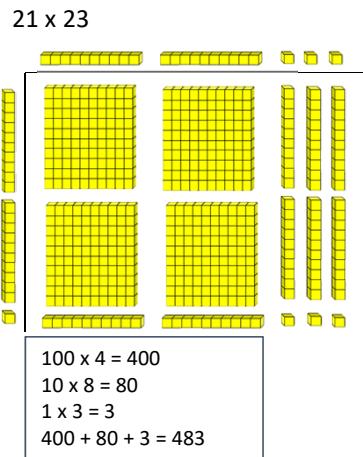
100       $100 + 20 = 120$

$10 \quad 10 \quad 10$   
 $1 \quad 10 \quad 10 \quad 10$   
 $1 \quad 10 \quad 10 \quad 10$   
 $1 \quad 10 \quad 10 \quad 10$

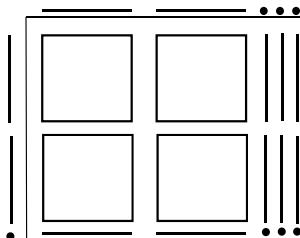
100       $100 + 20 = 120$

$40 \quad 40 \quad 40$   
 $40 \times 3 = 120$

This is where we start to see an increase in students efficiency in thinking.

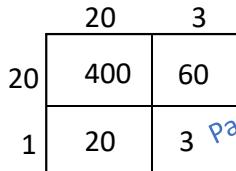


Pictorial Representation



$10 \quad 10 \quad 1 \quad 1 \quad 1$   
 $10 \quad 10 \quad 10 \quad 10 \quad 10$   
 $10 \quad 10 \quad 10 \quad 10 \quad 10$   
 $10 \quad 10 \quad 1 \quad 1 \quad 1$

$400 + 80 + 3 = 483$



$400 + 60 + 20 + 3 = 483$

Keep increasing the efficiency and maintain the accuracy



## Multiplication Progression

23  
 $\underline{\times} 21$   
 $3 (1 \times 3)$   
 $20 (1 \times 20)$   
 $60 (3 \times 20)$   
 $400 (20 \times 20)$   
 483

Students have built **conceptual understanding** and now starting to understand **procedurally**.

23  
 $\underline{\times} 21$   
 $23 (1 \times 23)$   
 $460 (20 \times 23)$   
 483

Students will start to develop more efficient ways of thinking abstractly.

You may choose to go into a standard algorithm at this point but it is not required!