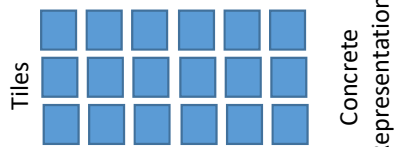


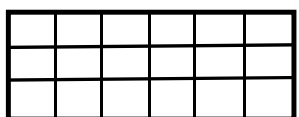
Multiplication starts when students are asked to partition a square 5 by 5.

Repeated addition = Multiplication
 $5 \times 5 = 25$

Students will construct arrays using square tiles or any manipulative..

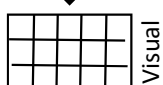


When students create the concrete representations they should also be drawing visual representations as well



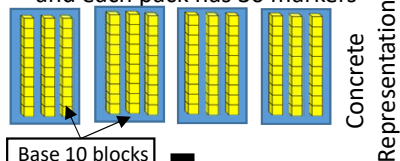
\times \div
 Relational Thinking
 $15 \div 3 = \square$
 $3 \times \square = 15$
 $? = 5$

Use concrete representations to draw understanding and build concepts

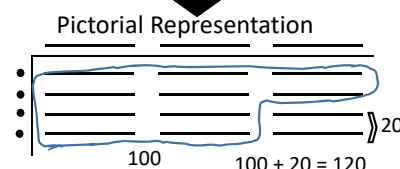
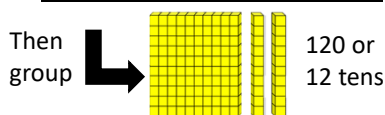
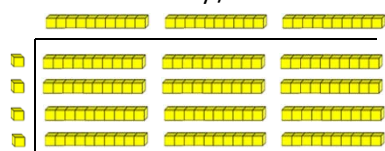


Example Problem:

There are 4 packs of markers and each pack has 30 markers



Create an array / Area model

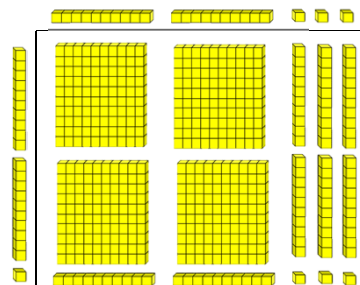


$$\begin{array}{r} 10 \quad 10 \quad 10 \\ 10 \quad 10 \quad 10 \\ 10 \quad 10 \quad 10 \\ 10 \quad 10 \quad 10 \\ \hline 100 \quad 100 \quad 100 \\ 100 + 20 = 120 \end{array}$$

$$\begin{array}{r} 10 \quad 10 \quad 10 \\ 4 \quad 40 \quad 40 \quad 40 \\ \hline 40 \times 3 = 120 \end{array}$$

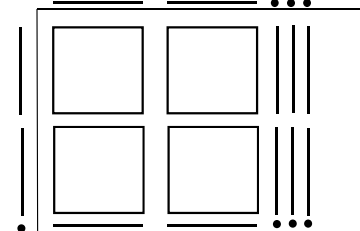
This is where we start to see an increase in students efficiency in thinking.

21×23



$$\begin{array}{l} 100 \times 4 = 400 \\ 10 \times 8 = 80 \\ 1 \times 3 = 3 \\ 400 + 80 + 3 = 483 \end{array}$$

Pictorial Representation



$$\begin{array}{r} 10 \quad 10 \quad 1 \quad 1 \quad 1 \\ 10 \quad 100 \quad 10 \quad 10 \quad 10 \\ 10 \quad 100 \quad 10 \quad 10 \quad 10 \\ 1 \quad 10 \quad 10 \quad 1 \quad 1 \\ \hline 400 + 80 + 3 = 483 \end{array}$$

$$\begin{array}{r} 20 \quad 3 \\ 20 \quad 400 \quad 60 \\ 1 \quad 20 \quad 3 \\ \hline 400 + 60 + 20 + 3 = 483 \end{array}$$

$$400 + 60 + 20 + 3 = 483$$

Keep increasing the efficiency and maintain the accuracy



Multiplication Progression

$$\begin{array}{r} 23 \\ \times 21 \\ \hline 3 \quad (1 \times 3) \\ 20 \quad (1 \times 20) \\ 60 \quad (3 \times 20) \\ \hline 400 \quad (20 \times 20) \\ 483 \end{array}$$

Students have built **conceptual understanding** and now starting to understand **procedurally**.

$$\begin{array}{r} 23 \\ \times 21 \\ \hline 23 \quad (1 \times 23) \\ 460 \quad (20 \times 23) \\ \hline 483 \end{array}$$

Students will start to develop more efficient ways of thinking abstractly.

You may choose to go into a standard algorithm at this point but it is not required!

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 Adapted from: Graham Fletcher